## Microfabrication of Transformers and Inductors for High Frequency Power Conversion

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Abstract— Transformers and inductors fabricated with micron-scale magnetic-alloy and copper thin films are proposed for high-frequency power conversion applications. Fine patterning produced by photolithography reduces eddy current losses, resulting in very high power densities. Calculated design graphs and design examples for 10 MHz transformers are presented.

### I. INTRODUCTION

One of the main difficulties in the miniaturization of power conversion circuits such as dc to dc converters is the construction of inductors and transformers. Increased switching frequency can, in general, lead to decreased requirements for the values of inductors and capacitors in power circuits. Transformer size can also be decreased at high frequency because of the reduced volt-seconds across each winding. However, as frequencies are pushed into the MHz region, several problems arise. Core materials commonly used in the 20-500 kHz region, such as MnZn ferrites, have rapidly increasing hysteresis and eddy current loss as the frequency is increased. Furthermore, eddy current loss in windings can also become a severe problem, as the skin depth in copper becomes small in relation to the diameter of wire used. Even if these problems are adequately dealt with, the resulting transformer and/or inductor is still one of the physically largest components, and is likely to cost the most to manufacture.

In the magnetic recording industry, thin-film metal alloys are replacing ferrites as the material of choice for inductive read-write heads, particularly where high-density and high frequency are required. These materials have high saturation flux density, and the use of thin films controls eddy current losses at high frequencies, up to frequencies above 100 MHz [1, 2, 3]. Structures with very small feature size are fabricated with integrated-circuit-like photolithography techniques [4, 5, 6, 7]. The materials and the fabrication techniques used for magnetic recording heads show much promise for high-performance highfrequency power conversion. The ability to accomplish very fine patterning can reduce eddy-current losses in both cores and windings. The higher saturation flux density of the magnetic alloys, as compared to that of ferrites, allows high power density in small, planar devices. While costs may initially be high, mass production techniques could conceivably bring the cost down to lower levels than conventional wound magnetic circuit elements. In any case, the cost structure will be very different, with cost related to the number of layers and substrate area, rather than the volume of magnetic material and complexity and number of turns, as is the case with conventional magnetics. This may mean that components needing a large number of turns will be more practical with microfabrication techniques.

Much previous work has been done on the design of planar high-frequency power transformers. However, most of it uses relatively large-scale fabrication techniques, and uses ferrite cores. In [8], however, a power transformer is constructed using a thin (10  $\mu m$ ) metal film core. It achieves an efficiency of 78%, but at a low power density,  $3 mW/cm^2$ . In [9], a transformer fabricated with sputtered CoZrRe core material achieves higher power density of about  $0.72 \ W/cm^2$ . In this paper, we discuss design and optimization procedures for high frequency transformers using thin film microfabricated transformers. Our results show that much higher power densities and efficiencies are possible in an optimized transformer, constructed using materials and processes similar to those used to construct magnetic recording heads. Design and optimization approaches for high frequency transformers using these materials and processes are developed. Efficiency and power throughput are estimated for a range of designs, and are worked out in detail for one example design.

Microfabricated magnetic components are expected to be useful for a wide range of applications. Our results are given in terms of power handling capability per unit substrate area for a specified efficiency level, and can be used for any power level, simply by scaling the area. For high-power applications, a substrate might have the power semiconductors, capacitors, and control circuitry mounted on one side, and the microfabricated magnetics fabricated on the reverse side. Since the magnetics would be less than 100  $\mu m$  thick, a heat sink could be mounted on the same side of the substrate as the magnetics. Substrates with microfabricated magnetic devices could also be stacked to increase power handling. For low-power applications requiring a few watts, microfabrication would make it possible to use a transformer only a few millimeters square, allowing the entire converter to fit in a very small package.

It would also be desirable to be able to integrate magnetic components onto a silicon substrate along with other control and power circuitry. This would, for example, allow a power circuit to be added to a VLSI circuit, making the chip entirely self-sufficient, without requiring external support in the form of power supplies. Integration of a power circuit, even if it were for powering external circuitry or equipment, would offer advantages. For example, the short interconnections between

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the magnetic and other circuit elements would decrease the lead inductance which can otherwise cause problems at high frequencies.

Although we focus on power-handling magnetic components, there are potentially many other applications for microfabricated magnetic components. In power electronics, these applications could include small, high-Q inductors for resonant gate drive applications [10, 11]. The square hysteresis loop characteristic of the magnetic materials is ideal for magnetic amplifier applications and other devices requiring these characteristics, such as some current sensors [12].

#### II. MAGNETIC MATERIALS

Although ferrites are among the most popular materials for designing conventional high frequency transformers, they are not easily integrated with microfabrication methods. The high sintering temperatures of standard high quality ferrites (1000 to 2000 degrees centigrade [13]) are difficult to combine with other steps of microfabrication techniques. However, other materials may actually be more desirable. The main advantage of ferrite over typical magnetic metal alloys is ferrite's high resistivity, which keeps eddy current losses to manageable levels at high frequency. The eddy current losses in magnetic alloys, however, can be controlled by using the alloys in thin film form. Furthermore, ferrites can only be run at relatively low flux levels, both because they have low saturation flux densities, and because rapidly increasing hysteresis losses limit ac flux to typically less than 0.1 T at frequencies over 1 MHz. Magnetic alloys used in recording heads have saturation flux densities over 1 T, and usually can be operated close to this level without a loss penalty.

Probably the most common, and best understood alloy for thin film magnetics is permalloy, Ni<sub>80</sub> Fe<sub>20</sub>. It has a saturation flux density of 1.1 T, and in bulk form has a resistivity of 20  $\mu\Omega cm$  [14]. Films may be deposited by electroplating [15, 16, 17], sputtering, [18] and other methods.

It is well known in the field of thin film magnetics that hysteresis loss in permalloy films can, in principle, be eliminated if changes in magnetization proceed by coherent rotation of the magnetization in a single domain, instead of by domain wall motion. This is achieved by controlling the anisotropy effects. We will briefly outline the principles of this, based on the discussion in [19, 20]. Discussion of these effects is also contained in [21, 22]. If the film is deposited or annealed in a magnetic field, parallel to one axis in the plane of the film, it develops a uniaxial anisotropy that can be described by the anisotropy energy,

$$U_u = K_u \sin^2 \theta, \tag{1}$$

where  $\theta$  is the angle between the magnetization vector and the easy axis of magnetization determined by the applied field during annealing. The behavior of the film in an applied field can be understood by considering the energy including the anisotropy energy and the energy associated with the applied field,

$$U = K_u \sin^2 \theta - H_x M_s \cos \theta - H_y M_s \sin \theta, \qquad (2)$$

where  $H_x$  and  $H_y$  are the components of the applied field in the easy and hard axis directions, respectively. At a stable equilibrium,  $\partial U/\partial \theta = 0$ , and  $\partial^2 U/\partial \theta^2 > 0$ . The first derivative condition results in

$$H_k \sin \theta \cos \theta + H_x \sin \theta - H_y \cos \theta,$$
 (3)

where  $H_k$  is a constant defined as  $H_k = 2K_u/M_s$ . In general one might expect to find that multiple stable solutions would lead to a multiple-valued B-H curve. For an applied field in the hard axis direction, (3) reduces to  $H_y/H_k = \sin \theta$ , and so  $M_y =$  $\sin \theta M_s = M_s H_u / H_k$ . This holds for  $|H_u| < H_k$ , and results in the lossless hysteresis loop shown in Fig. 1. Although there are multiple solutions for  $\theta$ , they result in the same value for  $M_{\nu}$ . For an applied field in the easy axis direction, on the other hand, multiple solutions result in the multiple-valued, and so lossy, hysteresis loop shown in Fig. 2. For our applications the hard axis loop is preferred. In practice it is best to orient the hard axis a few degrees away from the expected direction of the applied field, to help maintain a single magnetic domain. Although the hysteresis loops shown in Figs. 1 and 2 were measured at low frequency, behavior at frequencies up to 100 MHz is very similar. Thus, coherent rotation can be used to almost completely eliminate hysteresis loss.

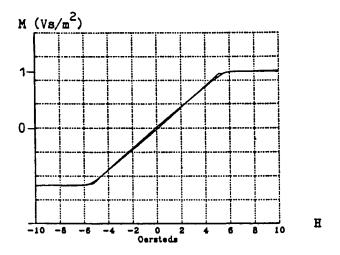


Fig. 1. Experimental NiFe hard axis hysteresis loop, from [20].

Another alloy commonly used for recording heads is sendust (FeAlSi). Its principal advantage for recording heads is its higher wear resistance, but it also has higher resistivity than NiFe, 90 to 119  $\mu\Omega cm$  [23, 24]. Numerous other materials are under development for higher performance magnetic recording heads. Although many of the requirements for magnetic recording heads are similar to those for power applications, in several respects, the requirements for power applications are less severe. In particular, mechanical wear resistance, corrosion resistance and thermal stability are all very important for magnetic recording heads. In power applications, however, the component is not subject to mechanical wear, and it can be sealed from the atmosphere to resist corrosion. Thermal stability is particularly important in Metal-In-Gap (MIG) recording heads, in which the high saturation flux density material is bonded at high temperatures to the main body of the core. Such a high temperature process would not be used in manufacturing power components. Thus some of the materials that are impractical for use in heads may be excellent for power

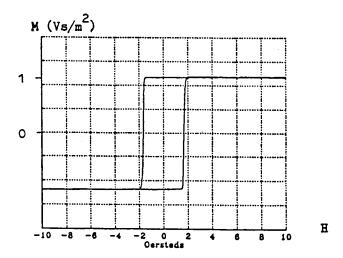


Fig. 2. Experimental NiFe easy axis hysteresis loop, from [20].

applications. For example, FeN compounds have shown saturation flux densities above 2.8T, and very low coercivity, under 0.3 Oe. The major drawbacks for recording head applications are its low corrosion resistance and low thermal stability. The addition of aluminum to these materials improves their thermal stability, while maintaining a high saturation flux density of 2T [25]. Many other materials being developed for recording head applications also show excellent coercivity and saturation flux density, and may be excellent for power applications [1, 2].

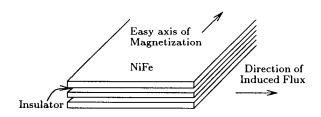


Fig. 3. laminated core structure.

In order to increase flux-carrying capacity without detrimental increases in eddy current loss, one may use layers of magnetic alloy, separated by a dielectric such as SiO<sub>2</sub> or AlO<sub>2</sub>, as shown in Fig. 3. In some recording-head materials, this also results in decreased coercivity [25, 1, 2]

## III. GEOMETRY

Any transformer, made by a process of alternately depositing conductor or magnetic material, must have have at least two steps of conductor deposition or two steps of core deposition in order to interlink the core and coil. Designs in either category may be considered variations or combinations of the basic constructions in Figs. 4 and 5, which we call pot-core and toroidal designs, respectively, because of their general resemblance to conventional pot-core and toroidal transformers.

In order to rigorously compare the power handling capabil-

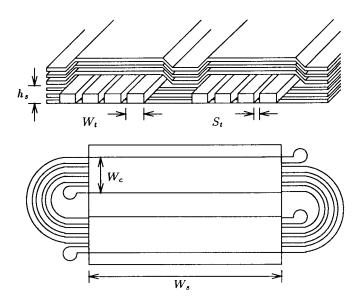


Fig. 4. "Pot-core" structure.

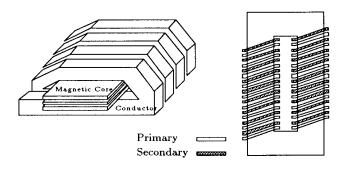


Fig. 5. "Toroidal" structure.

ity of the two designs, one must perform complete design optimization calculations, as discussed in the following sections. The result is that the pot core design can handle more power in the same area. In order to make this result more intuitive, we consider also a simpler situation. We compare a pot-core and a toroidal design, each with the same layer thicknesses: each conductor layer in the toroidal design the same as the one conductor layer in the pot-core design, and each core layer in the pot-core design the same as the one core layer in the toroidal design. As shown in Appendix A, at low power density, the two designs have the same efficiency, with the ratio of voltage and current in each set to maximize efficiency. However, with the same power density, the toroid has a higher flux density. It will be shown that optimal designs will always be limited by saturation. This can explain the higher power handling capability of the pot-core design.

Sometimes an important issue in choosing a core shape is the magnitude and distribution of external magnetic fields generated by the transformer. The pot core is often the best design for this because the core encloses and so shields the windings. The result is low external fields regardless of the distribution of primary and secondary windings inside the core. Toroidal transformers also often have low external fields. This is more a result of the winding distribution than of the core shape, however. The primary and secondary winding are customarily both distributed evenly around the core, lying on top of each other with little space between. Thus the currents, as seen from even a short distance away, very nearly cancel each other, and so little external field results. Secondarily, the effects of magnetizing current producing external fields are minimized because the MMF produced by the winding is dropped locally in the same portion of the core, and thus no two regions of the core are at MMFs that differ by more than the current in one turn.

In microfabricated transformers, ability to finely pattern windings makes it relatively easy to arrange the windings so that primary and secondary currents locally cancel. Thus the first advantage of toroidal-core transformers is easily realized, even in non-toroidal shapes. With a high-permeability core material such as NiFe, magnetizing current will be relatively small, making the second advantage of toroids unimportant. Thus external fields are not a concern in choosing geometry.

Perhaps the most important parameter to consider in comparing pot-core and toroidal designs is ease of fabrication. This is also the most difficult to quantify, but it appears that that pot-core design is overall easier to fabricate, as discussed below. It is also more similar to recording head designs, and so is better proven.

In the toroidal-core design, a difficulty is connecting the bottom and top layers of conductor to encircle the core. This requires that the registration between the layers is adequate to insure proper connections, requires low-resistance contacts, and requires connection over a vertical distance equal to the thickness of the core. None of these are beyond the capabilities of present technology, but all add some difficulty or complexity. The accuracy of registration required is on the order of the spacing between individual conductors running over the top. For our example design this spacing is  $5 \mu m$ . Registration accuracy better than this is not hard to achieve. Connections over the thickness of the core can be achieved by first smoothing the edges with insulator.

In the pot-core design, the inter-layer connection requirements are in one sense less severe, because connections to particular individual wires are not required, and small gaps of insulator would not be a problem as the area can be made sufficiently large that the gap reluctance is negligible. However, if the thickness of the conductor layers is larger than the thickness of the core layers (which will be the case in our designs) the vertical distance over which connections must be made is larger in the pot-core design. There is also an additional connection that must be made. Unless the transformer has only one turn, the winding will be a spiral, and there must be connections to the center of the spiral. This would typically involve a fourth deposition step, or the use of external connections such as bond wires. Series and parallel combinations of single-turn structures are a possible way to get around this problem.

In an NiFe toroidal core, the orientation of the easy axis of magnetization may be difficult. In a circular core, the desired easy axis direction is radial in a circular core. In a square core, there are only two different directions needed, but it would still be very difficult to achieve the precise localized fields needed to fabricate this. A long rectangular core could be used, with the easy axis oriented a few degrees from perpendicular to the length of the core. For most of the core, it would be properly oriented. However, for the ends of the core, it would be oriented in the wrong direction, resulting in high losses due to the easy-axis hysteresis loop. It should then be made as long and thin as is practical to minimize these end losses.

In the pot core design, the easy axis orientation is not difficult if, again, the shape is long and rectangular, with the turns going around the end uncovered by any core material, as shown in Fig. 4. A problem, however, is that the flux must cross perpendicular to the sheets to get from the top layers of NiFe to the bottom layers. Flux in this perpendicular direction will produce some eddy current losses.

Overall, the pot core design appears to be superior, because it can handle higher power, has fewer difficulties with interconnecting different layers of conductor, and can easily have the magnetic anisotropy oriented correctly.

## IV. WINDING DESIGN

In this section, design of transformer windings for the lowest possible loss is discussed, considering high frequency skin effect and proximity effect losses, and the limitations imposed by microfabrication techniques. Throughout this discussion it will be assumed that the actual number of turns is of little consequence. As long as the overall structure is large enough that there are many turns, the effective number of turns can be adjusted at will by putting turns in series or parallel, by making minor adjustments to the overall size, and even by putting entire micro-transformers in series or parallel. The parameter  $R/n^2$ , not R, is to be minimized.

We assume that it is necessary to fabricate the windings in a single layer for the pot core design, in order to minimize the cost. In this case, an important constraint in the winding design is the spacing between windings. This may be constrained by the vertical to horizontal aspect ratio achievable with the photolithography process used. For example, with a plated height of  $20~\mu m$ , and a 1:4 aspect ratio, the minimum spacing between conductor segments is  $5~\mu m$ . In some cases the minimum spacing may be set by other constraints, for example where very high voltage isolation or low capacitance between primary and secondary is needed. For example, SiO<sub>2</sub> has a dielectric strength between 300 and 1000 V/ $\mu m$  [26, 27]. A 5  $\mu m$  thickness may be adequate for some applications, but depending on the derating factor used and the voltage requirements, greater thickness may be needed.

Simple dc  $R/n^2$  minimization would dictate that the conductor should be as wide as possible, and the space between conductors as narrow as possible consistent with the constraint (e.g.  $5~\mu m$ ). However, for high frequency currents, skin effect becomes important, and when the conductor gets wide compared to the skin depth, it is not effectively utilized. Thus there is an optimal width, between very small widths where too much of the cross-sectional area is wasted by the interwinding space, and large widths where skin effect and proximity effect increase the losses. For both the pot-core and toroidal geometries under consideration, the skin effect and proximity effect losses can be approximated by an ac resistance, determined by multiplying the dc resistance by a factor  $F_r$ , which can be approximated

by,

$$F_r = 1 + \frac{5p^2 - 1}{45}\psi^4,\tag{4}$$

where p is the number of "layers," and  $\psi$  is the ratio of conductor thickness to skin depth [13, 28]. Completely interleaving primary and secondary windings is desirable, because p takes on its minimum value, one half. To minimize ac resistance, we adjust the width of the individual conductor turns,  $W_t$ , to minimize a resistance factor,  $F'_R$ , that takes into account both the reduction in conductor area due to spacing between windings,

$$F_r' = F_r \frac{W_t + S_t}{W_t},\tag{5}$$

where  $S_t$  is the spacing between turns, determined by the aspect ratio. At 10 MHz, for example, copper has a skin depth of 22  $\mu m$ , and  $F'_r$  takes on a minimum value of 1.18 with  $W_t = 34.3 \mu m$ , for  $S_t = 5 \mu m$ .

If more than one layer can be used for the winding, the primary and secondary may be wide ribbons, on top of one another. In this case the above optimization is unnecessary, but the fabrication requires more steps.

#### V. Laminations

Similar to losses in the conductor, eddy current losses in the core are decreased by making finer laminations, but making them fine also sacrifices cross-sectional area and so increases the flux density, which increases losses and can lead to saturation. An appropriate compromise must be found.

Eddy current power loss may be easily estimated if it is assumed that the field distribution is not affected by the induced current, and so is uniform throughout the cross section of the lamination. This is ordinarily a good assumption if the thickness of the lamination is thin compared to a skin depth. At 10 MHz the skin depth in NiFe with a permeability of 2000 is about 3  $\mu m$ . Furthermore, in thin films on the order of 1  $\mu m$ , the uniformity of the field is enhanced by spin coupling [20]. Thus the approximate form,

$$P_{loss} = \frac{\omega^2 B_{peak}^2 V d^2}{24\rho} \tag{6}$$

where V is the volume and d is the lamination thickness, is a good approximation.

Since the cost of fabrication is likely to be very dependent on the number of layers, we take the number of layers as given, and optimize the thickness of the layers. Given this, the cross sectional area and volume of core material are proportional to the thickness of the laminations. For a given total flux, B is inversely proportional to the thickness. Since B and the thickness of the laminations both appear squared in the loss, those terms cancel, and the only overall effect of thickness on total loss is through the volume term. Thus the thickness should be chosen as small as possible, consistent with avoiding saturation.

## VI. TRANSFORMER DESIGN

There are many possible design methodologies. For instance, one may choose a power throughput density objective, and find

the maximum efficiency design meeting that objective. Or one may start with an efficiency objective and find the maximum power throughput density possible at that efficiency. We will choose the latter, in part because it is easier to come up with an efficiency objective a priori.

With a winding height, winding spacing and width, and number of core layers fixed, the only important remaining choices for a rectangular geometry are the height of the core ( $h_s$ , s for steel), the voltage, the current, the width of the core  $(W_s)$ , and the width of the windings,  $(W_c, c \text{ for conductor})$ . In practice, there would be a fixed requirements for current and voltage, and the overall size and number of turns would be adjusted to match these. However, for the purposes of determining the throughput possible at a given efficiency, we will assume that the number of turns is fixed and adjust both the voltage and current. If the width of the windings and core are large enough, the throughput per substrate area becomes a very weak function of those widths. We can assume, for approximate calculations, that the edge and end losses are negligible, and so the efficiency and throughput are independent of Wc and Ws.

Any optimal design will have the flux density at the saturation flux density of the core, although in practice, some safety margin will be allowed. This is because if the flux density were below the maximum allowed, the voltage and current could be scaled up together, increasing the power handling without affecting the efficiency. Thus for any given core height, the optimal voltage is easily calculated. Given an efficiency requirement, the optimal core height (which determines an optimal voltage), and the maximum current for that efficiency, may be calculated. In Appendix B this is shown to result in a power density.

$$P/A = \frac{31104\sqrt{2}B^2w^2h_c^3(1-\eta)^5\rho_s^2N^4}{3125\pi^7\rho_c^3F_R'^3}$$
 (7)

for a transformer with square voltage waveforms and sinusoidal current waveforms. This expression is valid for laminations thin enough that the approximation of uniform B used to calculate eddy current loss is valid. It also assumes negligible hysteresis losses. Note that the power density is very sensitive to the conductor losses, as indicated by the appearance of the cubes of conductor resistivity, height, and  $F_R'$ . It is even more sensitive to the number of layers, N, and to the efficiency,  $\eta$ .

## VII. EXAMPLE DESIGNS

In this section, the design methods discussed in the last section are applied to pot-core transformer designs based on a plated permalloy core material with copper conductors. We consider transformer designs for a series resonant converter, operating at 10 MHz. The assumption of a series resonant converter is needed only to determine the current and voltage waveforms in the transformer. Performance with other types of converters would be similar.

The core height was limited to a maximum total height of each half of  $20 \ \mu m$ , and a maximum lamination thickness of  $3 \ \mu m$ . Copper plating height was limited to  $20 \ \mu m$ . A maximum flux density of 1 T was used. Although resistivity of thin films of plated copper is often higher than copper's bulk resistivity, a thickness of  $20 \ \mu m$  is sufficient to achieve a resistivity very

close to the copper's bulk resistivity of 1.7  $\mu\Omega$ -cm [29, 30, 31]. We conservatively base our designs on a resistivity of 2.0  $\mu\Omega$ -cm. Since the NiFe core material is in much thinner layers, a maximum of 3  $\mu m$  thick, it may have significant increase in resistivity. Nonetheless, we conservatively base our calculations on its bulk resistivity of 20  $\mu\Omega$ -cm.

Based on these assumptions, the calculations outlined in Appendix B were used to find power density as a function of efficiency. The results are shown in Figs. 6-8 for transformers with one, four, or ten layers of NiFe laminations. The number of layers has a strong influence on the performance. With one layer, power density ranges from under 10 mW/cm<sup>2</sup> at 95% efficiency to 25 W/cm<sup>2</sup> at 70% efficiency. With ten layers, 75 W/cm<sup>2</sup> is achievable at 95% efficiency, and over 1000 W/cm<sup>2</sup> is possible at 70% efficiency.

Figure 9 is based on the same type calculation, and shows the possibilities offered by a higher-resistivity magnetic material, such as sendust. Sendust's resistivity was taken as  $105~\mu\Omega$ -cm, and it was used at a maximum flux density of 1T. The calculated performance of a 4-layer transformer was almost as good as a 10-layer permalloy transformer.

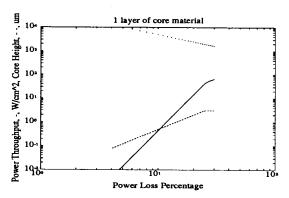


Fig. 6. Theoretical power throughput as a function of efficiency with a one-layer NiFe core in a pot-core design (solid line). Core height,  $h_{\pi}$ , for maximum power throughput is shown as a dashed line. The descending dotted line shows a thermal dissipation limit of 500  $W/cm^2$ .

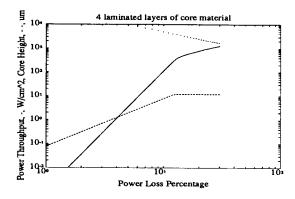


Fig. 7. Theoretical power throughput as a function of efficiency with a four-layer NiFe core in a pot-core design (solid line). Core height, and a thermal dissipation limit are also shown, as in Fig. 6.

To make the information shown in Figs. 6-8 more concrete, a design for a typical transformer has been performed and analyzed. Fig. 7 shows that a four-layer lamination can achieve

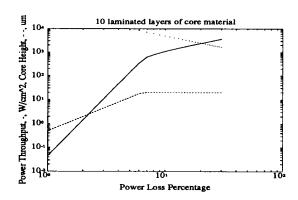


Fig. 8. Theoretical power throughput as a function of efficiency with a ten-layer NiFe core in a pot-core design (solid line). Core height, and a thermal dissipation limit are also shown, as in Fig. 6.

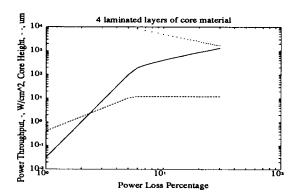


Fig. 9. Theoretical power throughput as a function of efficiency with a four-layer sendust laminated core (solid line). Core height, and a thermal dissipation limit are also shown, as in Fig. 6.

a power throughput of  $113W/cm^2$  at a theoretical efficiency of 90%. This is achieved with a lamination layer height of 1.97  $\mu m$ , for a total height of NiFe of 7.89  $\mu m$ . Dimensions are chosen for an approximate total substrate area of 5 mm by 1mm, and are adjusted to fit an integral number of optimal-width turns. Using the final dimensions shown in Table I, the actual efficiency and power density were calculated, and are also shown in Table 1. The actual efficiency includes hysteresis losses, and the losses in the end turns of conductor and in the overhang of the core. Hysteresis losses are assumed to be due to a parallelogram hysteresis loop with coercivity of 0.3 Oe. The magnetizing current was also calculated, but due to the high permeability of the NiFe, it contributes only a negligible amount to the conductor loss. The substrate area is the area of a rectangle enclosing the entire structure, including the end turns and core overhang. Leakage inductance and capacitances are based on simple one-dimensional field approximations, and SiO<sub>2</sub> dielectric.

#### VIII. POWER DISSIPATION

Often an important parameter in power transformer design is the allowable temperature rise, determined by power dissipation and thermal resistance, typically from the transformer to the surrounding air. Small transformers (on the order of 10 cm<sup>3</sup>) are typically limited more by efficiency requirements

TABLE I
Parameters of Example Design

Symbol		Value
$W_c$	Width of conductor	467 mm
$W_t$	Width single turn	$34.3~\mu m$
$S_t$	Spacing of turns	$5.0~\mu m$
$W_s$	Width of core	$5.0 \ mm$
$h_c$	Height of conductor	$20.0~\mu m$
$h_s$	Height of core	$7.89~\mu m$
$h_d$	Thickness of dielectric between conductor and core	$5 \mu m$
N	Number of layers of core	4
n	Number of turns in primary = number of turns in secondary	6
$\boldsymbol{A}$	Substate area	$0.0606\ cm^2$
f	Operating frequency	10 MHz
$\boldsymbol{B}$	Peak flux density	1.0 T
$ ho_c$	Conductor (Cu) resistivity	$2.0~\mu\Omega-cm$
$\rho_s$	Core (80% NiFe) resistivity	$20~\mu\Omega-cm$
$\mu$	Core permeability	$2000~\mu_0$
$\boldsymbol{P}$	Power throughput	6.06 W
P/A	Power throughput density	$100  W/cm^2$
	Eddy current loss in core	256~mW
	Hysteresis loss in core	76 mW
R	DC resistance (of either winding)	$2.03~\Omega$
$R_{ac}$	AC resistance	$2.09~\Omega$
	Total conductor losses	.530 $W$
$C_c$	Common-mode capacitance	19 <i>pF</i>
$C_s$	Self Capacitance (each winding)	11 pF
$L_{l}$	Total leakage inductance	61 nH
$L_m$	Magnetizing Inductance	$7.1~\mu H$
$i_m$	Magnetizing Current	$42~mA~{ m rms}$
i	Current (in primary and secondary)	.357~mA
	Total conductor losses	530~mW
v	Voltage	18.9~V
η	Efficiency	86 %

than by temperature rise. This is also true of the microfabricated transformers discussed here. Typical power semiconductors are rated to dissipate about  $500~W/\mathrm{cm}^2$ . With similar mounting and heatsinking techniques, similar power dissipation should be possible for microfabricated transformers. Dissipation of  $500~W/\mathrm{cm}^2$  is far above the typical dissipation of our designs of around  $10~W/\mathrm{cm}^2$ . Figs. 6-9 show a  $500~W/\mathrm{cm}^2$  limit as a dotted line. Only very low-efficiency, high-power-density, many-layered designs exceed this limit.

## IX. INDUCTORS

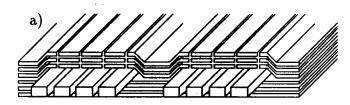
Inductors are also essential in switching power converters. Perhaps the simplest way to build a microfabricated inductor would be to use the pot-core geometry, and introduce a gap between the top and bottom sections of core. Unfortunately,

this "sandwich" design leads to very high eddy current losses in the conductor, because of the distribution of the field in the region of the windings [32, 33, 34]. For ac inductors, this has led to the use of "meander coils" [35, 36, 37] which are effectively many single-turn structures in series. Since a single-turn inductor does not have proximity effect problems, this is effective in decreasing losses. However, in order to effectively utilize the magnetic material and in order to get a high inductance, the gap reluctance in the magnetic path around each conductor must be reasonably small [35]. In microfabricated designs, this would require spacing the conductors widely enough to allow the top layer of magnetic metal to come down close to the bottom layer. This decreases the area available for conductor, and so increases the area needed for the complete device. Nonetheless, it is a viable option.

Proximity effect losses in a multi-turn planar pot-core inductor can be almost completely eliminated by using a lowpermeability material across the top of the windings, to serve the function of a gap, and maintain a favorable field configuration for low losses in the windings [34]. One way of making relatively low permeability core materials is to finely powder a magnetic alloy, and then press the powder into a core. This puts in many small air gaps. A problem with this is that the grains of magnetic material are randomly shaped and spaced, and as a result some portions have higher flux densities than others. This makes linearity and low loss hard to achieve. With microfabrication techniques, the gaps could be put in much more exactly, achieving better characteristics. An equivalent of lower permeability material can be made by simply putting small gaps at regularly spaced intervals, forming a quasi-distributed gap. Fig. 10 shows examples of such a design for a microfabricated inductor. This is similar in concept to the quasi-distributed gap used in [38], but microfabrication makes the use of multiple gaps easier, and the planar structure makes them more important. Fabricating the gaps by overlapping layers of magnetic material, as shown in Fig. 10 b may make precise control of very small gap lengths easier. A twodimensional finite-element magnetic field analysis was used to evaluate the losses in a structure like Fig. 10 a, operated at 10 MHz. Spacing between conductors, and between the conductors and the core was 5  $\mu m$ , the gaps were each 1  $\mu m$ , and each conductor was 35  $\mu m$  wide by 20  $\mu m$  high. The core was assumed to be ideal, lossless material 8  $\mu m$  thick. The conductor losses were only 8% higher than the dc losses with the same current, corresponding to a value of  $F_R$  of 1.08. This shows that the design does in fact control eddy current losses very effectively. For comparison, a similar geometry, but with the gap at one edge only, had losses nearly over four times as high.

## X. Conclusions

Microfabricated magnetic components with NiFe or other metal-alloy cores show much potential as components in high-frequency power converters. The high saturation flux density of these materials, combined with the ability to reduce eddy current losses by making microscopic laminations, allows very high power densities to be achieved. A pot-core-like structure with multiple horizontal layers of alloy, separated by insulator, appears to be the most desirable configuration. A design methodology is developed for choosing optimal conductor



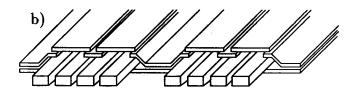


Fig. 10. Microfabricated inductors with quasi-distributed gap.

widths, and core height. The approximate range of power density with a ten-layer core includes over 1000W/cm<sup>2</sup> at 70% efficiency, and 95% efficiency at 75W/cm<sup>2</sup>. An example design is worked out in detail, and achieves 86% efficiency at 100W/cm<sup>2</sup> with a four-layer core.

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### APPENDIX

## A. COMPARISON OF LOSS IN POT-CORE AND TOROID-CORE STRUCTURES

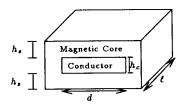


Fig. 11. Basic geometry considered.

First consider a section of copper surrounded by core, as shown in Fig 11. We assume that the conductor path is closed, but ignore any deviations from the above geometry where the core turns corners. We also ignore any core loss in the sections at the left and right edges. We calculate the resistance and flux density:

$$R = \frac{\ell \rho}{dh}.$$
 (8)

$$B = vt/\ell h_s \tag{9}$$

where t is the time of one quarter period of a square voltage waveform

$$P_{coreloss} = 2K_{core}B^2\ell h_s d \tag{10}$$

where  $K_{core}$  is a loss constant for the core material

$$P_{total loss} = \frac{2K_{core}dt^2v^2}{\ell\hbar_*} + i^2R \tag{11}$$

For a given transformer VA, P, the loss is minimized at

$$v = \left(\frac{t^2 \rho P^2 h_*}{d^2 h_c t^2 2 K_{core}}\right)^{1/4} \tag{12}$$

which results in loss

$$P_{total \, loss} = 2\sqrt{2} \, t P \sqrt{\frac{K_{core} \rho}{h_s \, h_c}} \tag{13}$$

and flux density

$$B = \left(\frac{\rho P^2 t^2}{2d^2 h_c h_s^3 K_{core} \ell^2}\right)^{1/4} \tag{14}$$

Now consider a section of core surrounded by copper with the identical geometry, except with  $h_c$  and  $h_s$  swapped so that  $h_c$  is still the conductor height and  $h_s$  is still the core height.

$$R = \frac{2d\rho}{\ell h_c} \tag{15}$$

$$P_{total loss} = \frac{K_{core} \ell t^2 v^2}{dh_*} + i^2 R; \tag{16}$$

For a given Transformer VA, P, the loss is minimized at

$$v = \left(\frac{2d^2\rho P^2 h_s}{\ell^2 h_c t^2 K_{core}}\right)^{1/4} \tag{17}$$

which results in exactly the same loss,

$$P_{total \, loss} = 2\sqrt{2}tP\sqrt{\frac{K_{core}\rho}{h_s h_c}}, \qquad (18)$$

but results in a higher flux density, by a factor of the square root of two,

$$B = \left(\frac{2\rho P^2 t^2}{d^2 h_c h_s^3 K_{core} \ell^2}\right)^{1/4} \tag{19}$$

Note that interchanging  $h_{\mathfrak{o}}$  and  $h_{\mathfrak{o}}$  makes no difference in the loss, but does affect the flux density.

# B. CALCULATION OF OPTIMUM CORE HEIGHT AND MAXIMUM POWER THROUGHPUT FOR A GIVEN EFFICIENCY

We perform this calculation for a horizontal-sheet-lamination potcore design such as in Fig. 4. Given an efficiency,  $\eta$ , and assuming a core height,  $h_s$ , we calculate the maximum current density,  $\sigma$ , which gives that efficiency or better, based on a similar geometry to that shown in Appendix A, ignoring all end and edge effects.

$$W_*h_*B = vt \tag{20}$$

$$t = \frac{\pi}{2\alpha} \tag{21}$$

$$P/A = \frac{2\sqrt{2}}{\pi} \frac{vi}{W.W.} = \frac{\sigma h_* \omega}{\pi^2} 4\sqrt{2}B \tag{22}$$

where  $W_s$  is the width of the core, and  $W_c$  is the width of conductor, as shown in Fig. 4, and  $\sigma = i/W_c$ . The factor of  $2\sqrt{2}/\pi$  results from assuming a square voltage waveform and a sinusoidal current waveform, as in a series resonant converter. If the number of layers of laminations N (per section, 2N overall for a pot core), the thickness of each layer is  $h_s/N$ .

$$P_{loss}/A = \frac{2h_s h_s^2/N^2 \omega^2 B^2}{24\rho_s} + F_R' 4\sigma^2 \rho_c/h_c$$
 (23)

The factor of two in the first term is due to the two sections of core in a pot core.  $F_R'$  is a resistance factor taking into account both the ac resistance factor  $F_R$ , and the loss of winding space due to gaps between turns. The factor of four in the second term is due to the fact that there are two windings, each with twice the resistance that a single winding occupying the same space would have. Setting  $(1-\eta)$  equal to the loss divided by the power throughput gives

$$\left(\frac{F_R' 4\pi \rho_c}{h_c h_* \omega}\right) \sigma^2 - 2B(1 - \eta)\sigma + \frac{h_*^2 B^2 \omega \pi}{12\rho_* N^2} = 0 \tag{24}$$

Solving this quadratic equation for  $\sigma$  gives

$$\sigma = \frac{h_c h_s \omega}{8\pi \rho_c F_R'} \left[ 2B(1-\eta) + \sqrt{4B^2 (1-\eta)^2 - \frac{4\pi^2 F_R' B^2 \rho_c h_s}{3h_c N^2 \rho_s}} \right]$$
(25)

where we have chosen the large valued root, because we want to choose the largest current, and so power density, at which the chosen efficiency is achieved. The power per area is then calculated by substituting  $\sigma$  into (22), to get

$$P/A = \frac{2\sqrt{2}}{\pi} \frac{h_c h_s^2 \omega^2 B_s}{4\pi^2 \rho_c F_R'} \left[ 2B_s (1-\eta) + \sqrt{4B_s^2 (1-\eta)^2 - \frac{4B_s^2 F_R' \pi^2 \rho_c h_s}{3h_c N^2 \rho_s}} \right]$$
(26)

To find the optimal value of  $h_s$ , we set the derivative of this expression with respect to  $h_s$  equal to zero, obtaining

$$h_{*opt} = \frac{72B_{*}^{2}(1-\eta)^{2}\rho_{*}N^{2}h_{c}}{25\pi^{2}\rho_{c}F_{R}^{\prime}B_{*}^{2}}.$$
 (27)

Substituting this into (26) results in an expression for the power density with the optimal value of  $h_s$ ,

$$P/A = \frac{31104\sqrt{2}B^2w^2h_c^3(1-\eta)^5\rho_s^2N^4}{3125\pi^7\rho_o^3F_R'^3}.$$
 (28)

For generating Figs. 6-9, the maximum  $h_s$  was constrained to  $20~\mu m$ , and the maximum thickness per lamination was constrained to  $3~\mu m$ . If those constraints were violated,  $h_s$  was set to the maximum, and (26) used to calculate the power density.